



# Analog and Digital Simulation of Microgrid Dynamics

James L. Kirtley Jr.  
Jorge Elizondo Martinez  
Po-Hsu Huang  
Colm O'Rourke  
Massachusetts Institute of Technology  
[kirtley@mit.edu](mailto:kirtley@mit.edu)

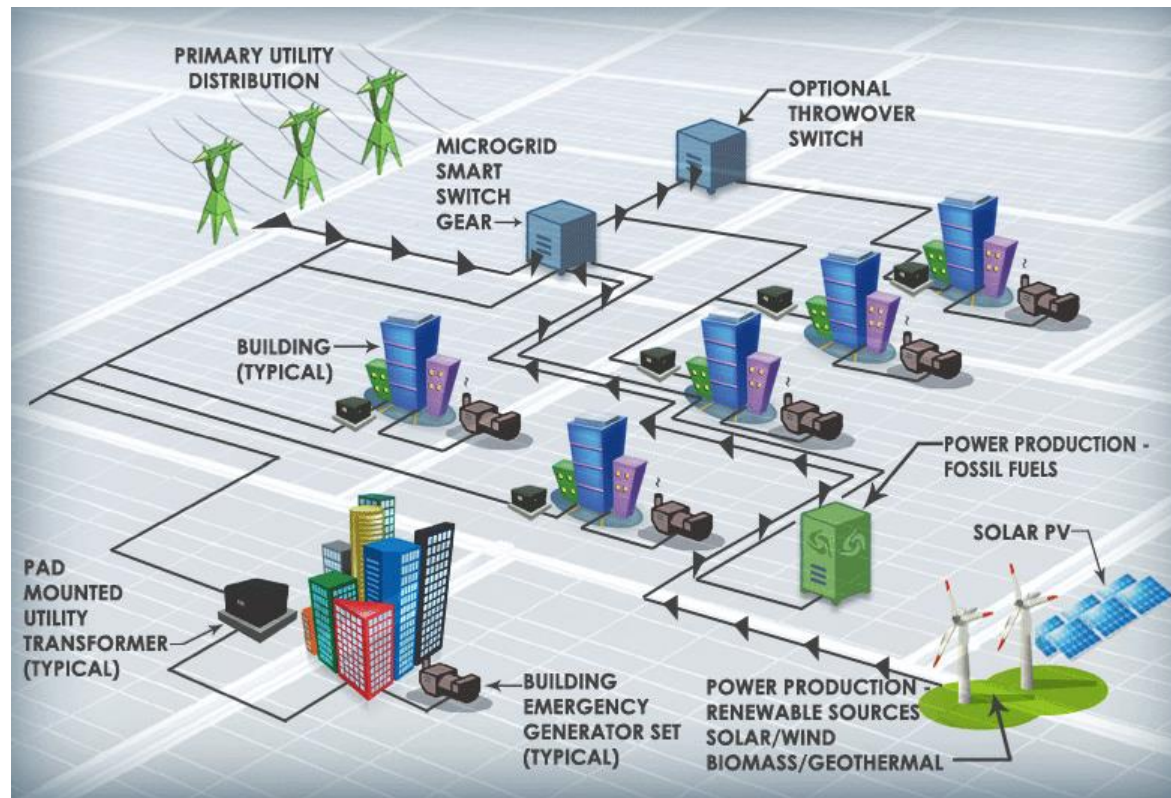


A Microgrid is either:

- A fragment of a power system
- A small power system

That can:

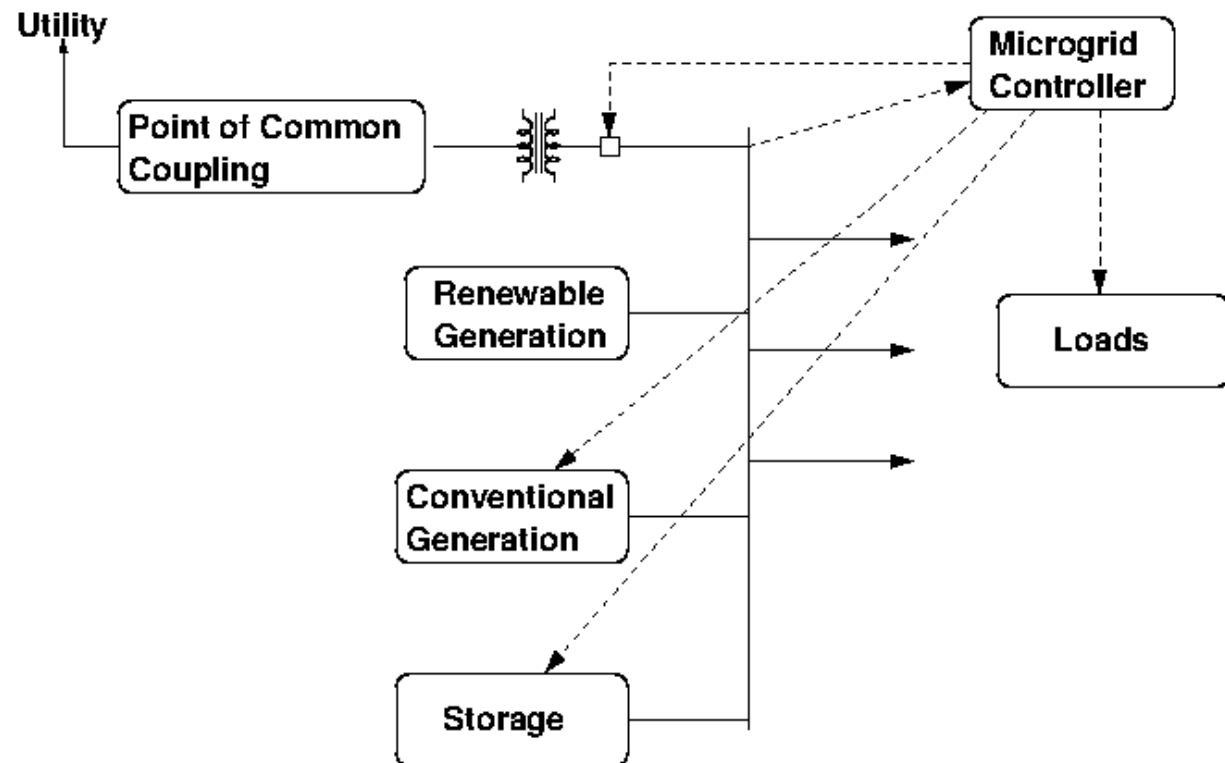
- Operate as a standalone system, or
- Operate in parallel with a large utility system

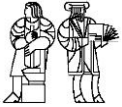




## What is the role of a 'Microgrid'?

- Enhance Reliability?
- Facilitate incorporation of renewable generation?





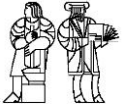
## Important issues related to microgrids:

### Local Generation:

- Renewables: Solar and Wind  
Difficult to Control and Dispatch
- Cogeneration: Combined Heat and Power  
Dispatch and Control have other worries
- Conventional generation gives a little bit of a break
- Some generation is provided through inverters  
Even if controllable, has no inertia  
And may current limit

### Loads

- Some loads may be responsive to system needs
- Some loads are constant power
- Some loads are constant impedance
- Induction Motor loads may be large and have special dynamics



## Enhanced Reliability:

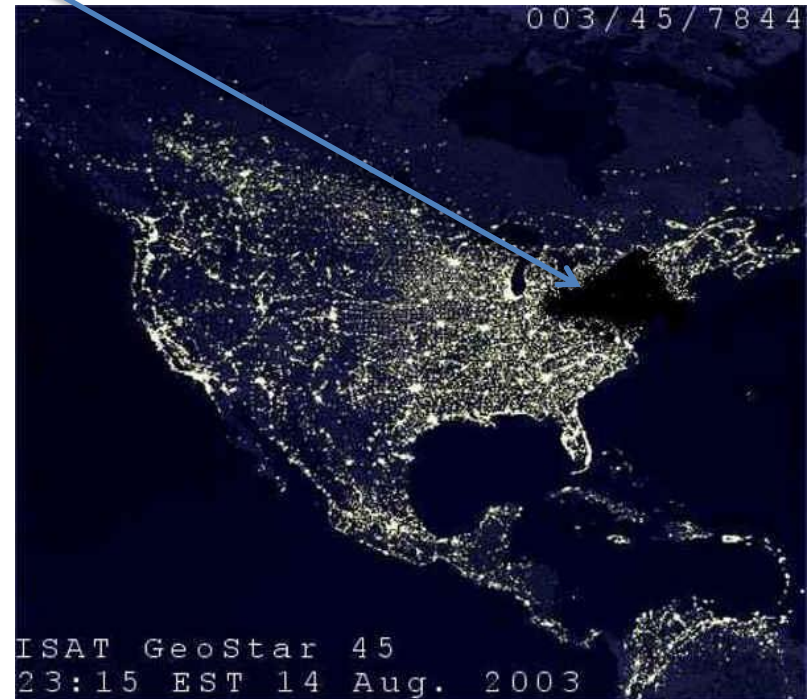
- Something goes wrong
- Not always as bad as this
- Examples:

Aggressive trees  
Vehicle accidents  
Weather

May require islanding

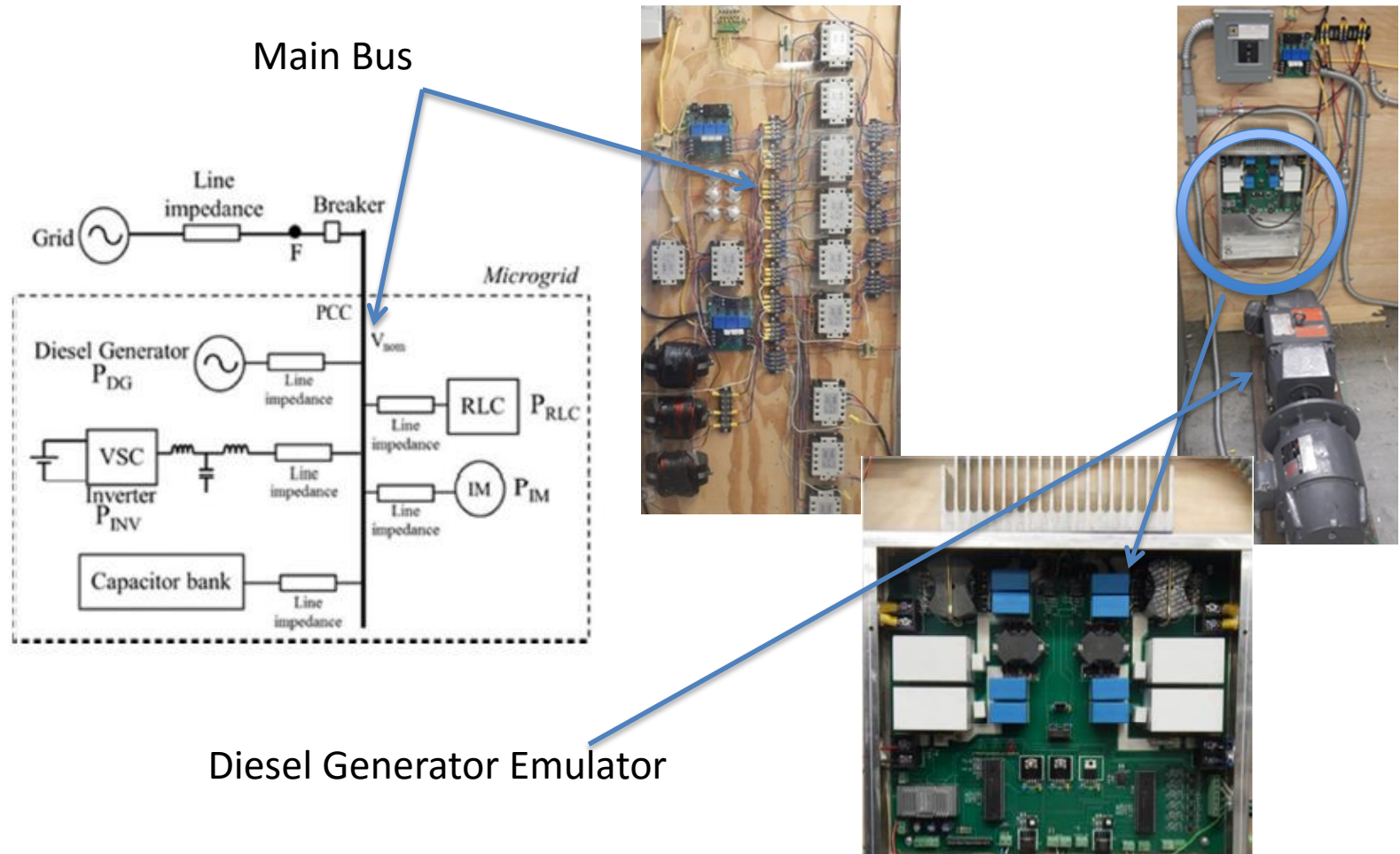
Control must:

- Detect the problem
- Determine if 'ride through' is possible, and if not:
- Shut down connection at PCC
- Balance load with local generation
- Existence of local storage can help with this





## Studies of Microgrids at MIT: an Emulator with Physical Machines and Electronics



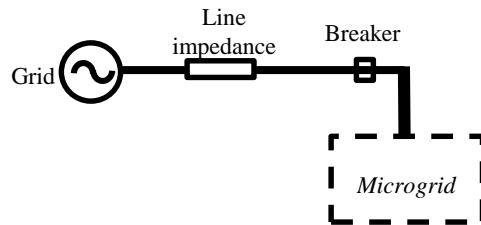




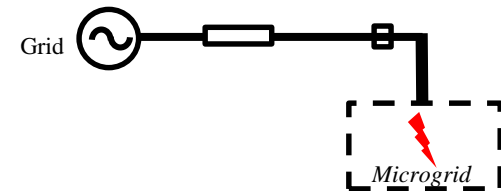
**INDUCTION MOTOR**  
**INDUCTION INSTRUMENTS**  
*LabVIEW™ Student Edition*



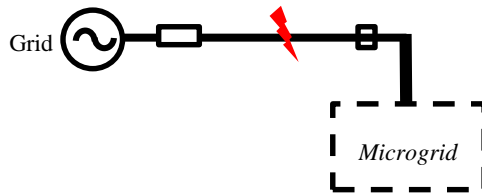
## Fault Sequences Under Study



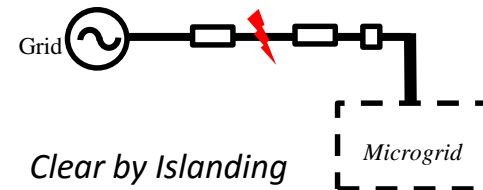
*Grid Connected Operation*



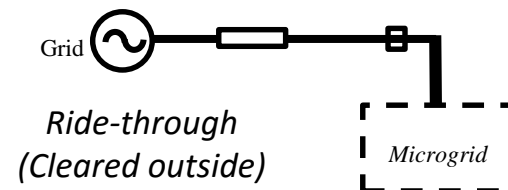
*Fault inside Microgrid*



*Fault outside Microgrid*



*Clear by Islanding*

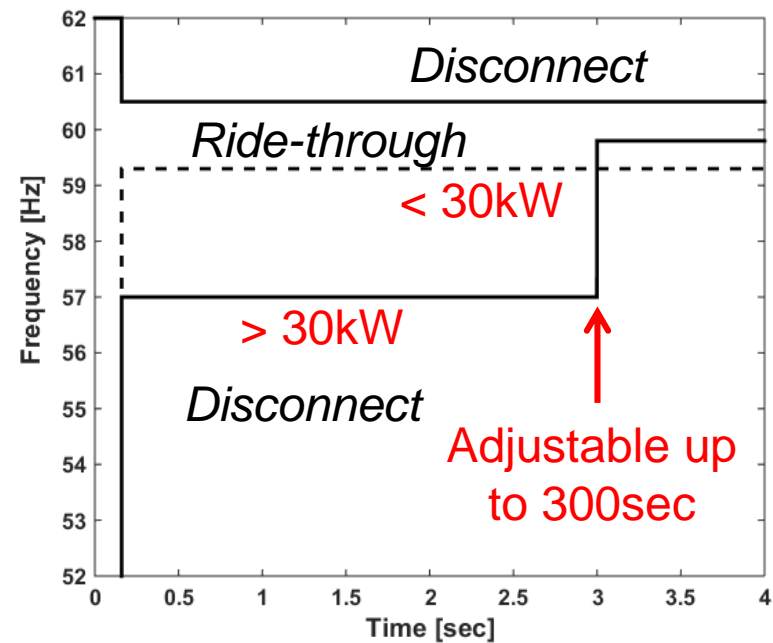
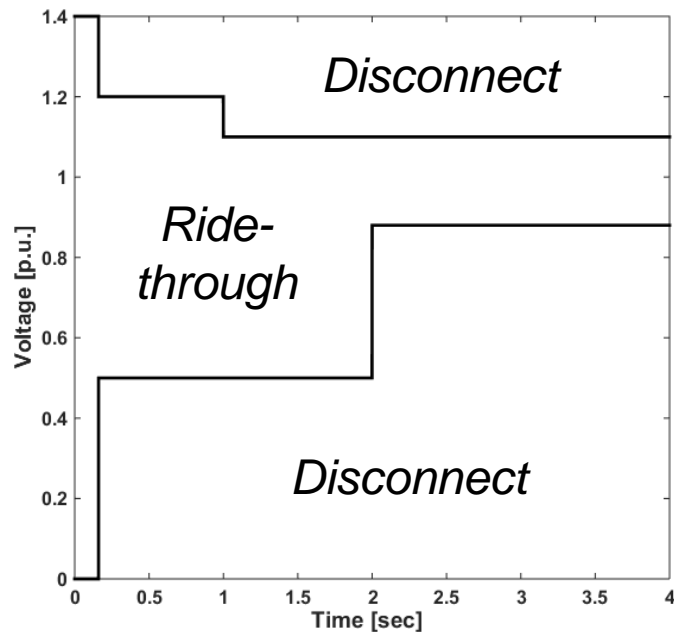


*Ride-through  
(Cleared outside)*



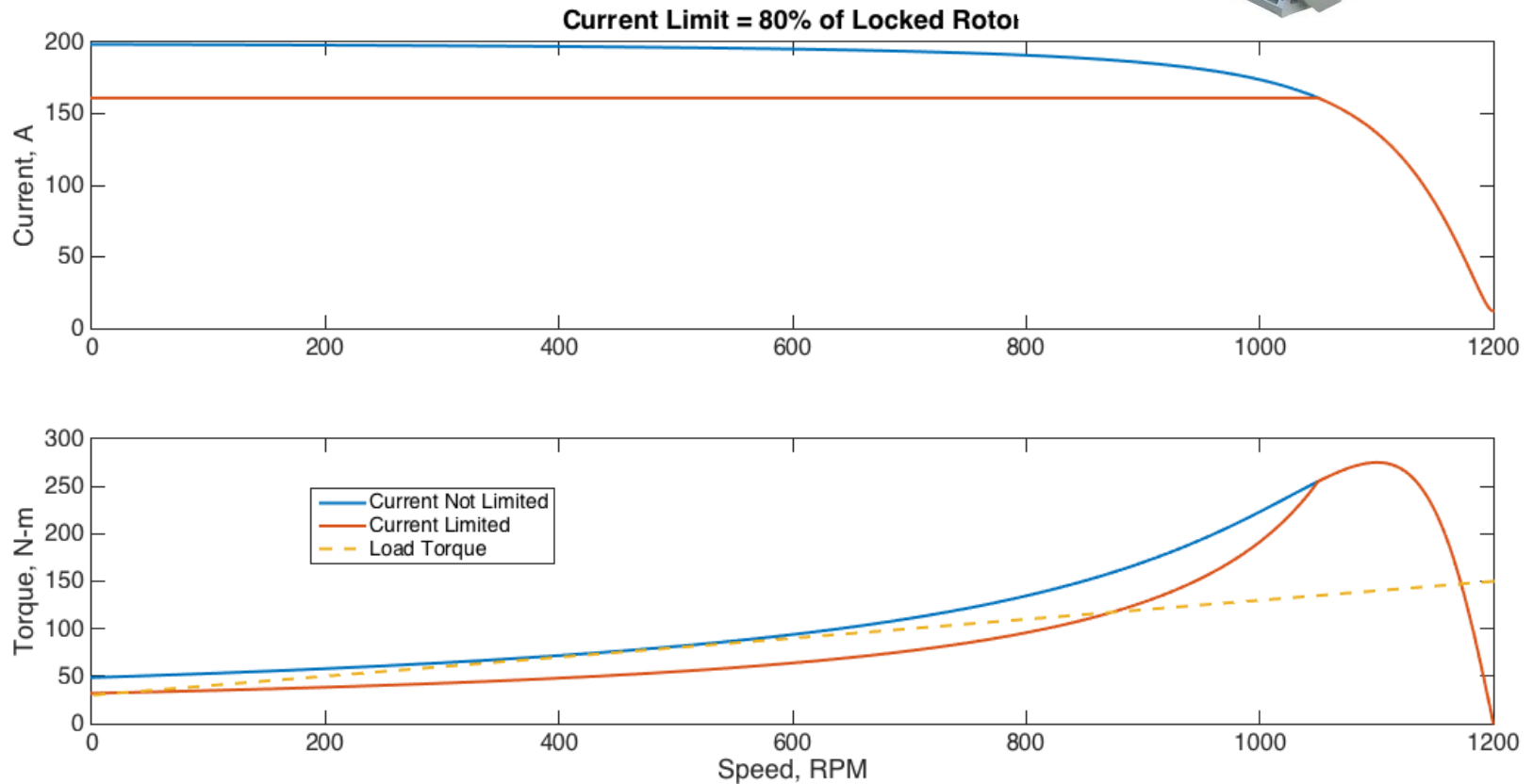
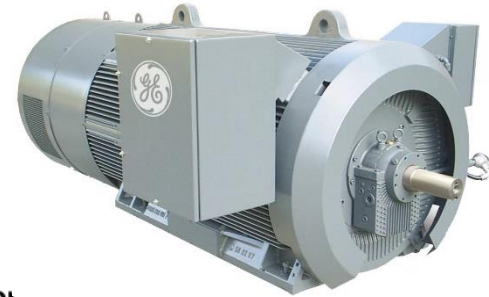


## IEEE Fault-Ride Recommendation





Consider an induction motor, torque and current vs. speed  
If current limited, torque is reduced over part of the speed range

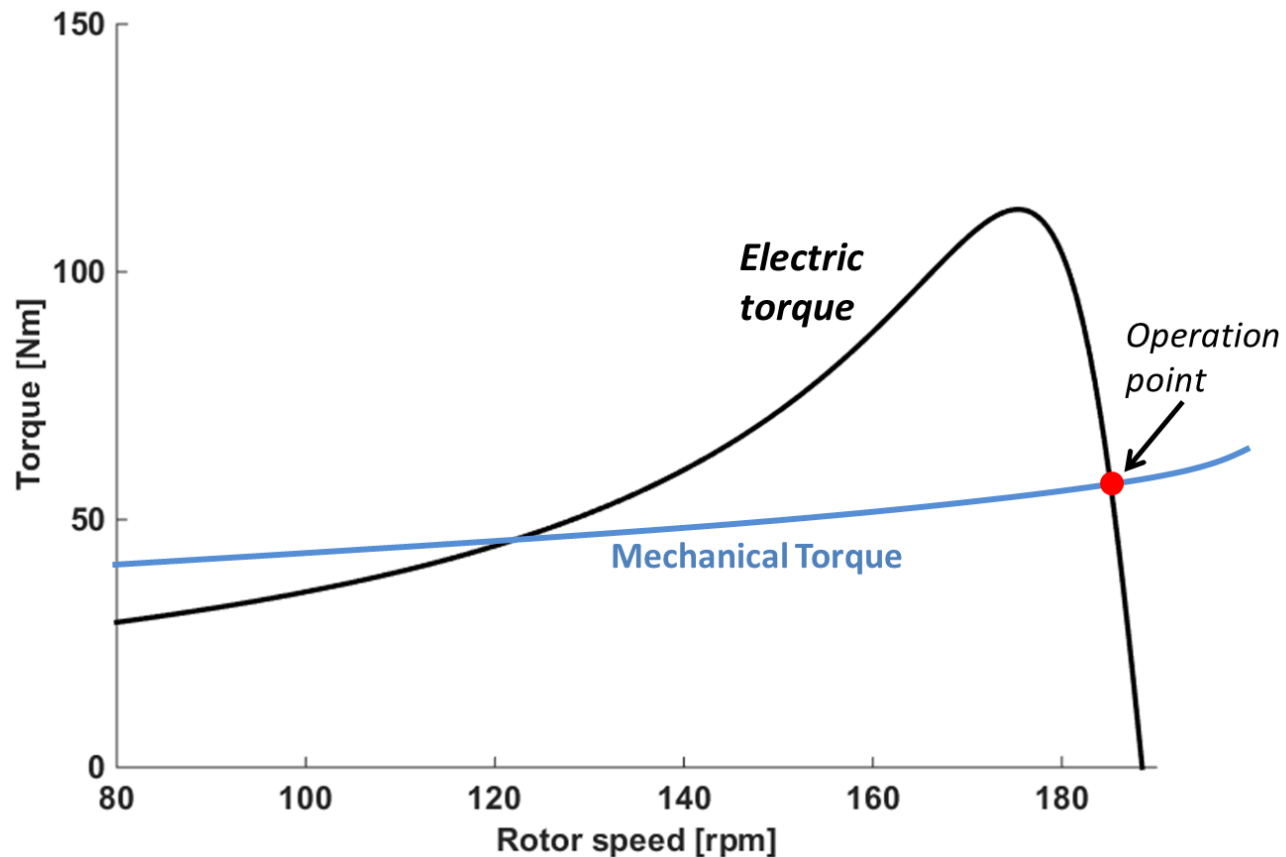




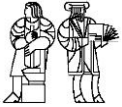
Pre-fault



## Torque-speed curve



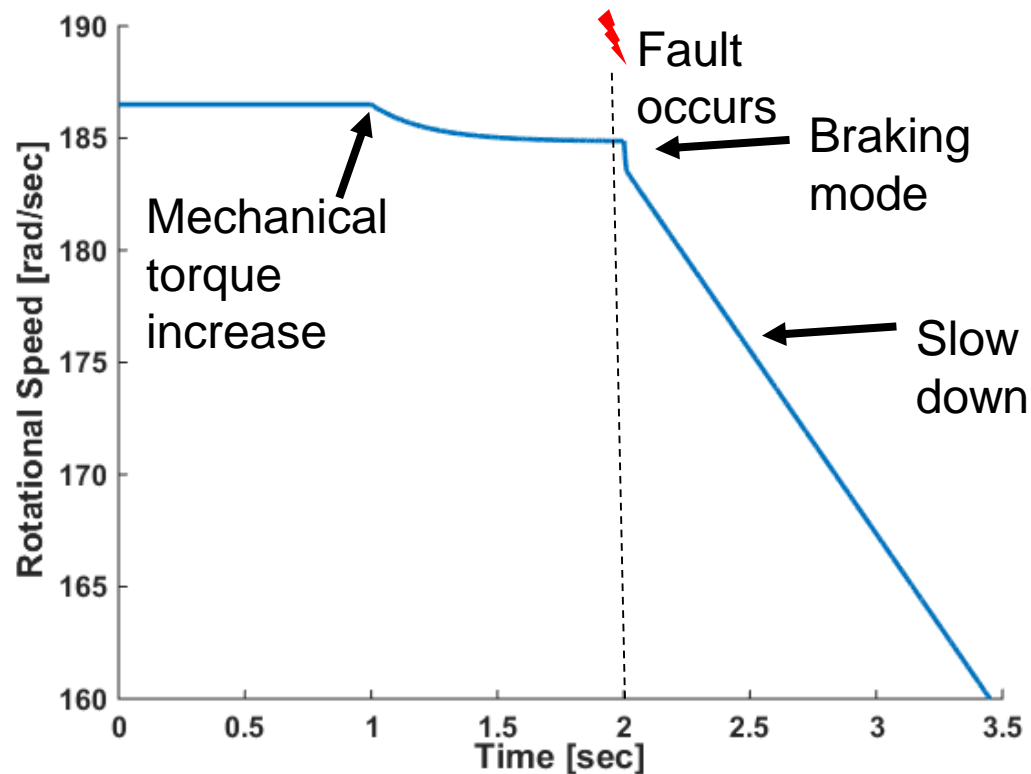
Intersection of the mechanical and electrical torques gives the operation point

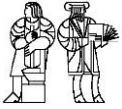


## During fault

At the moment of the fault, two phenomena occur:

1. Braking mode – IM dissipates its trapped flux
2. Slow down due to mechanical torque





## Detail of Simulation during a fault

### Dynamics

Electrical  
dynamics

$$\frac{d}{dt}\lambda_{ds} = v_d + \omega_0\lambda_{qs} - R_s i_{ds}$$

$$\frac{d}{dt}\lambda_{qs} = v_q - \omega_0\lambda_{ds} - R_s i_{qs}$$

$$\frac{d}{dt}\lambda_{dr} = (\omega_r - \omega_0)\lambda_{qr} - R_r i_{dr}$$

$$\frac{d}{dt}\lambda_{qr} = -(\omega_r - \omega_0)\lambda_{dr} - R_r i_{qr}$$

Mechanical  
dynamics

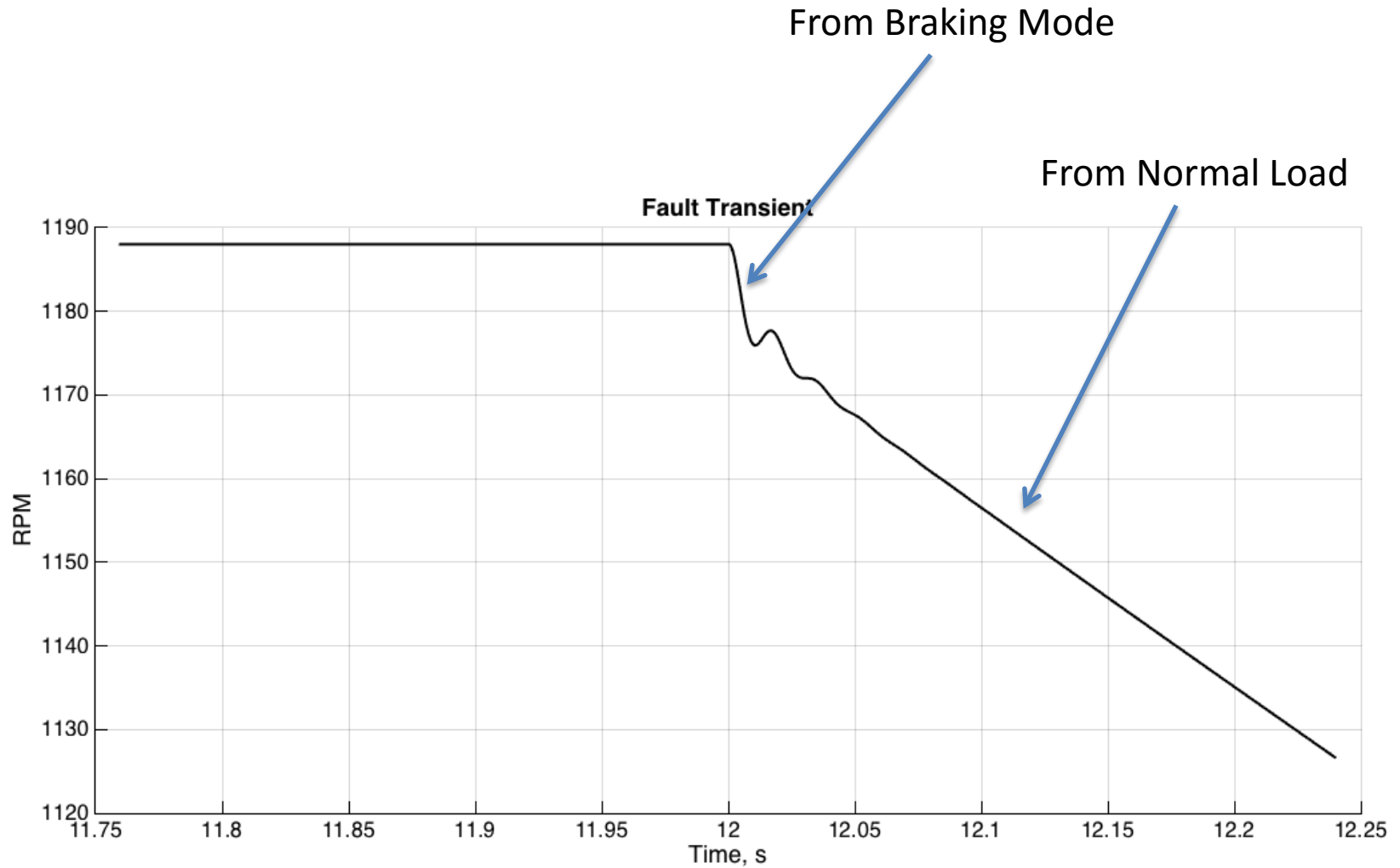
$$\frac{d}{dt}\omega_r = \frac{1}{J} (T_e - T_m - F\omega_r)$$

$$T_e = \frac{3}{2}p (\lambda_{ds} i_{qs} - \lambda_{qs} i_{ds})$$

$T_m$  depends on the mechanical load



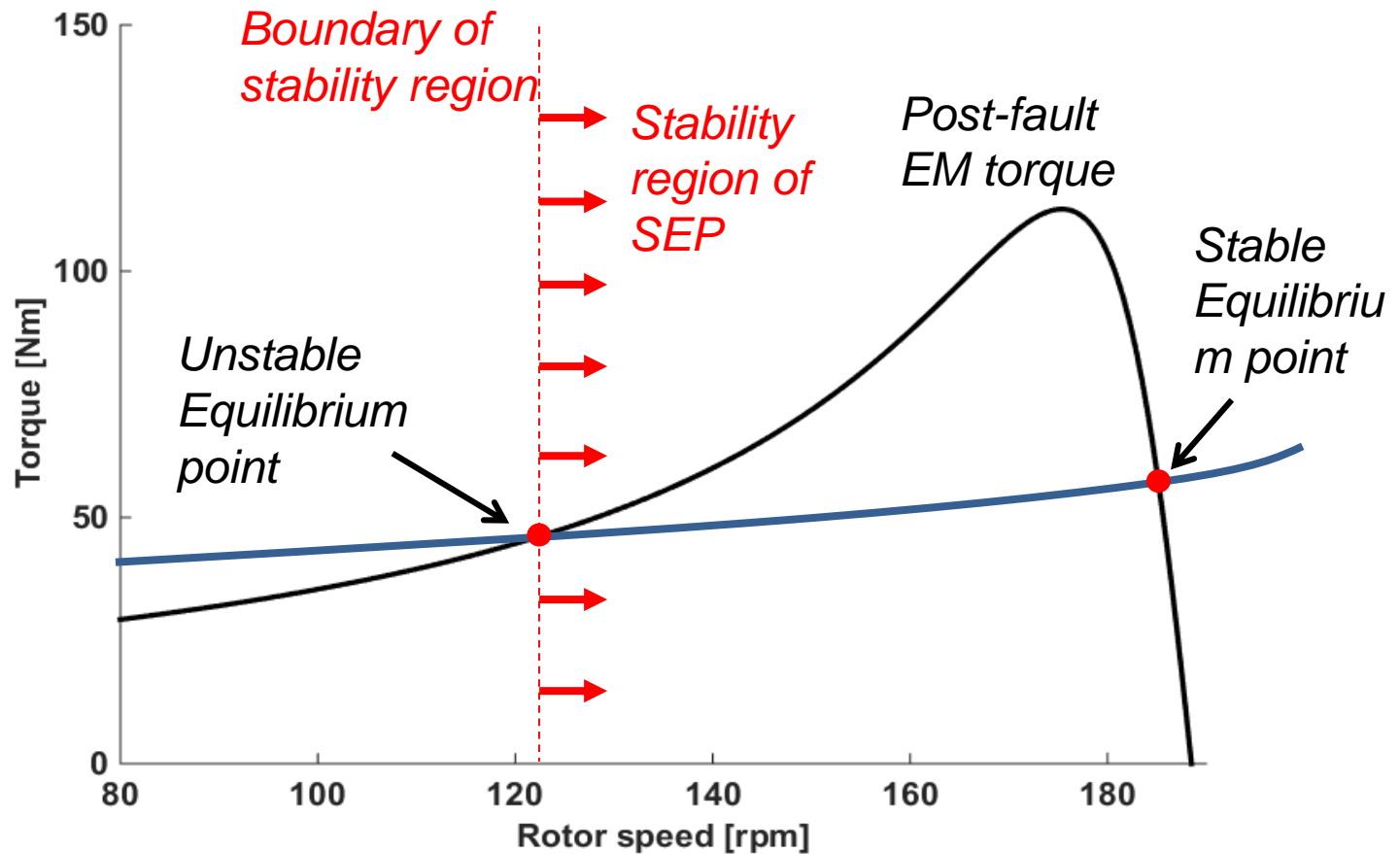
## Detail of simulation of Induction Motor Fault Behavior





## Post-fault

After the fault, the IM has electromagnetic torque returns

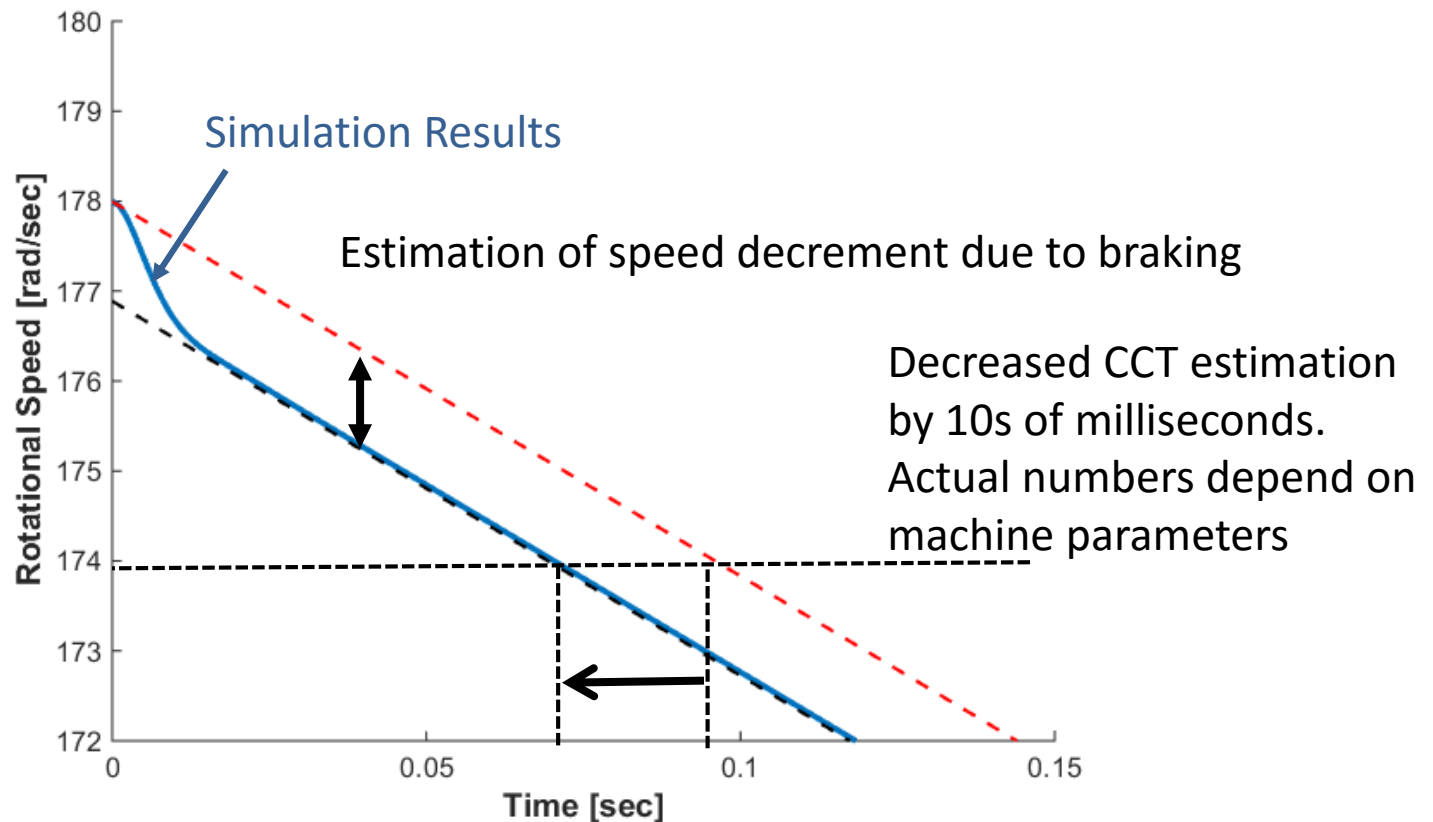






## Braking Mode Analysis

Method gives a good estimation of real speed decay

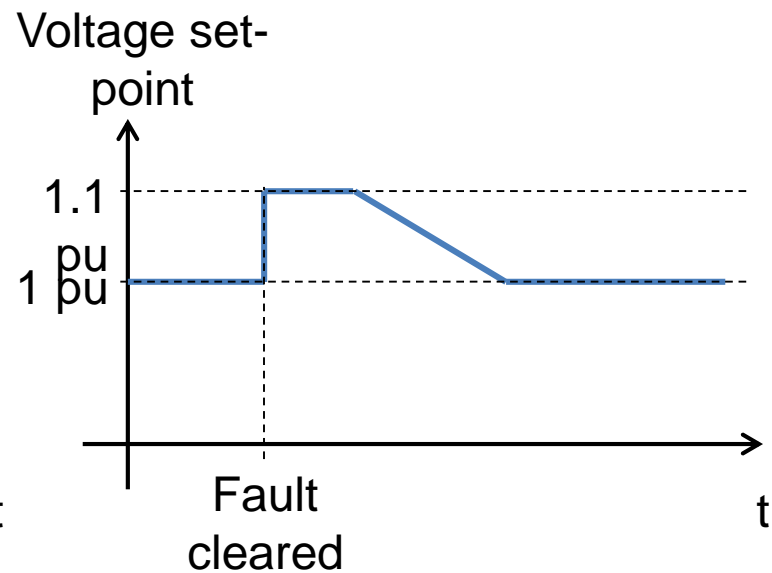
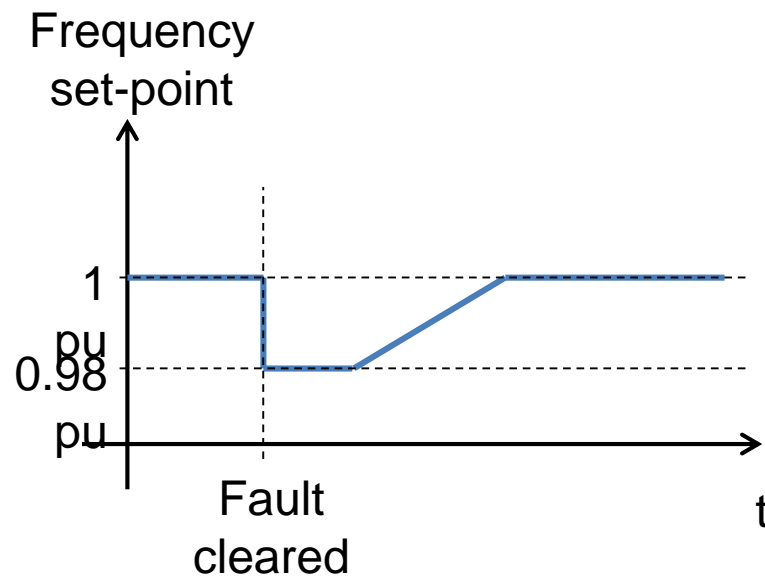




## Proposed Control Method

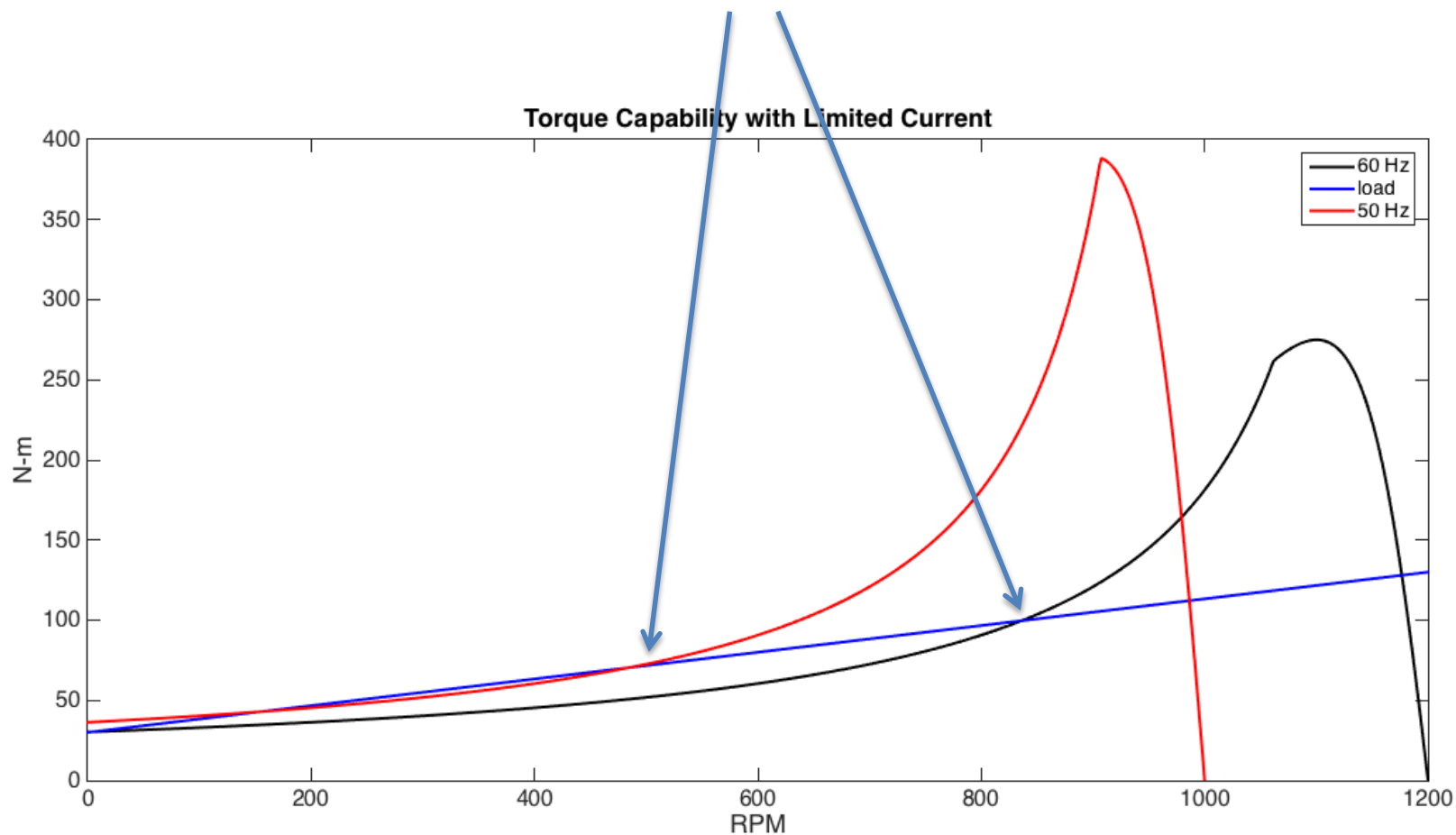
Take Advantage of the inverter  
Can Adjust Frequency and Voltage

Challenge the paradigm that a system has to recover to nominal conditions  
Instead, recover to “advantageous” conditions:



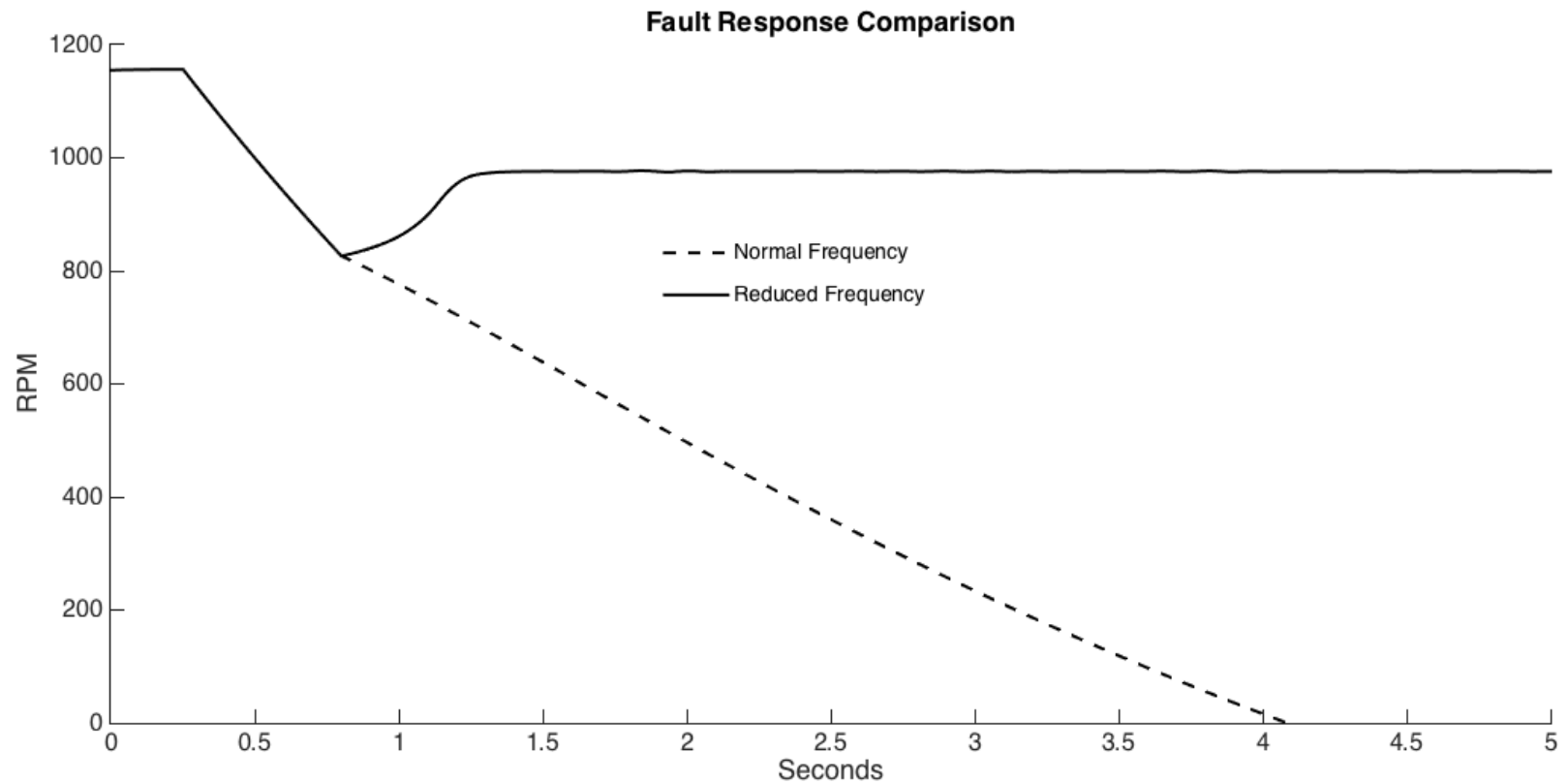


## Effect of Frequency Reduction Current Limited Conditions Difference in Clearing Time



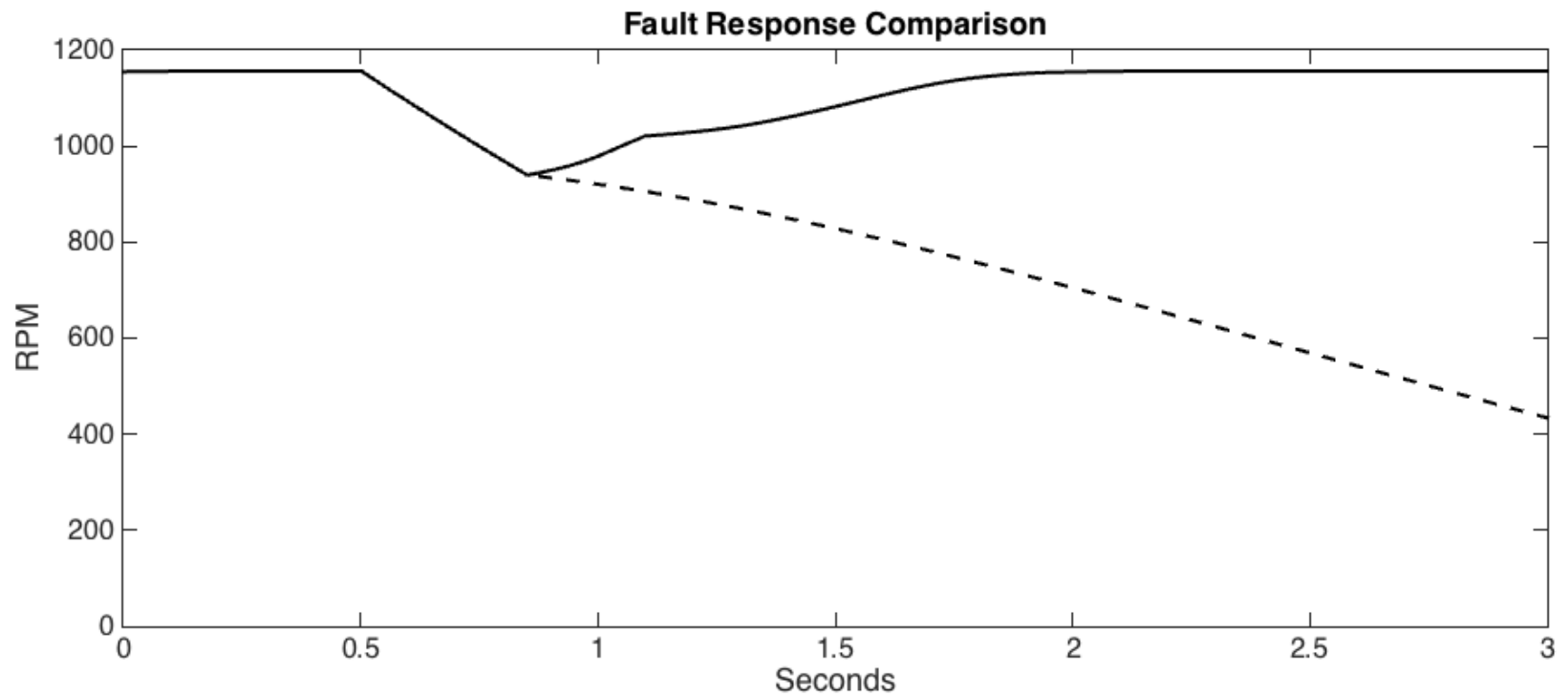


## Simulation of a Cleared Fault Recovery





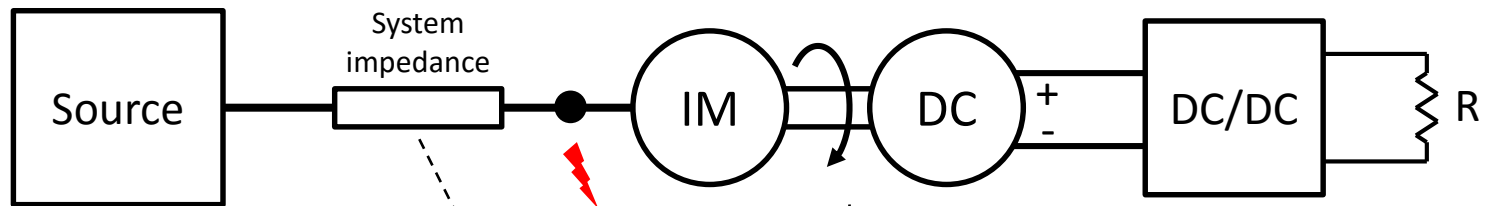
Or with a fairly rapid return to normal frequency

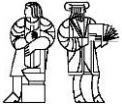




## Experimental Results

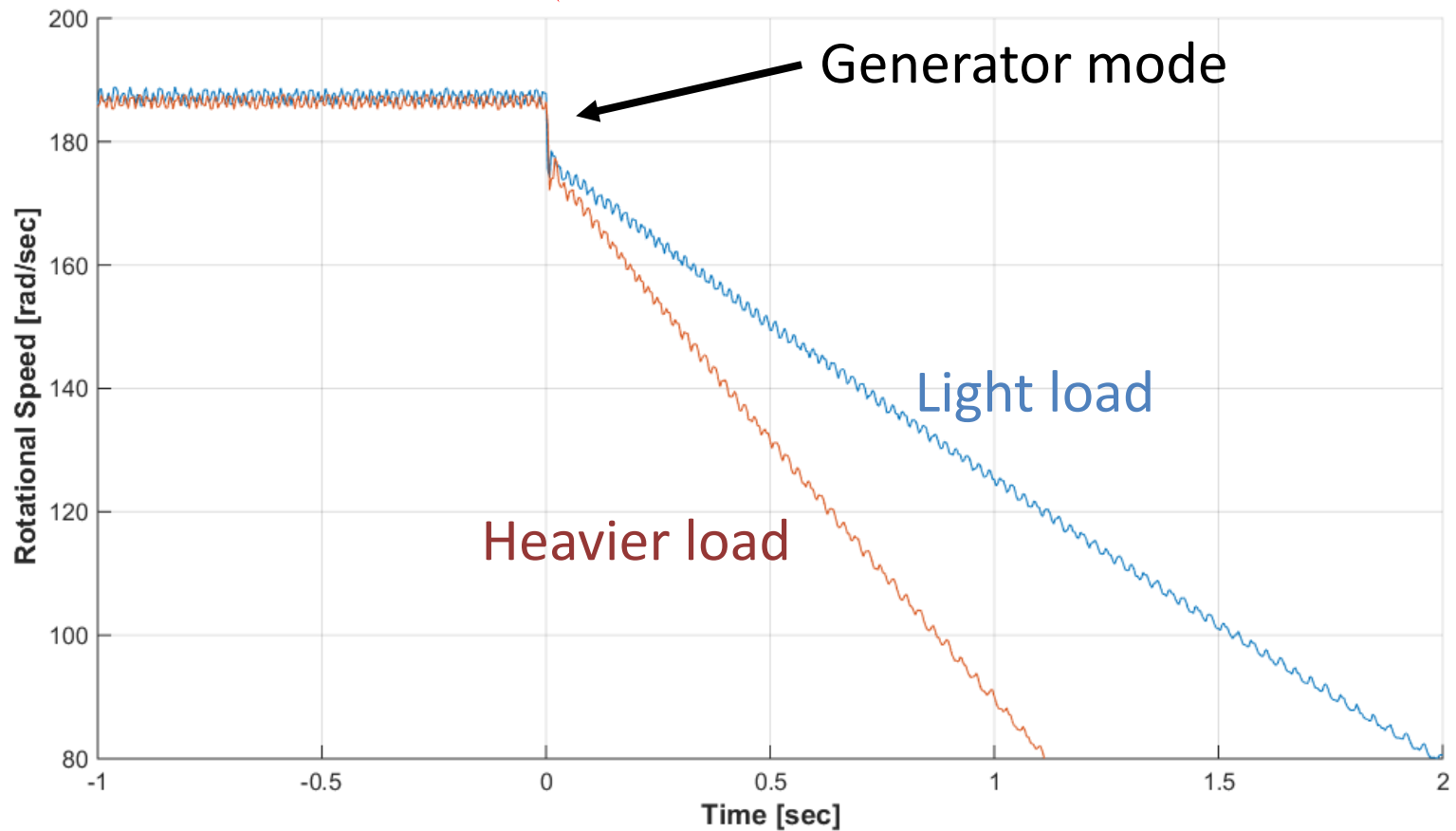
### Microgrid Experimental set-up





## Dynamics after the fault

Fault occurs at  $t = 0$

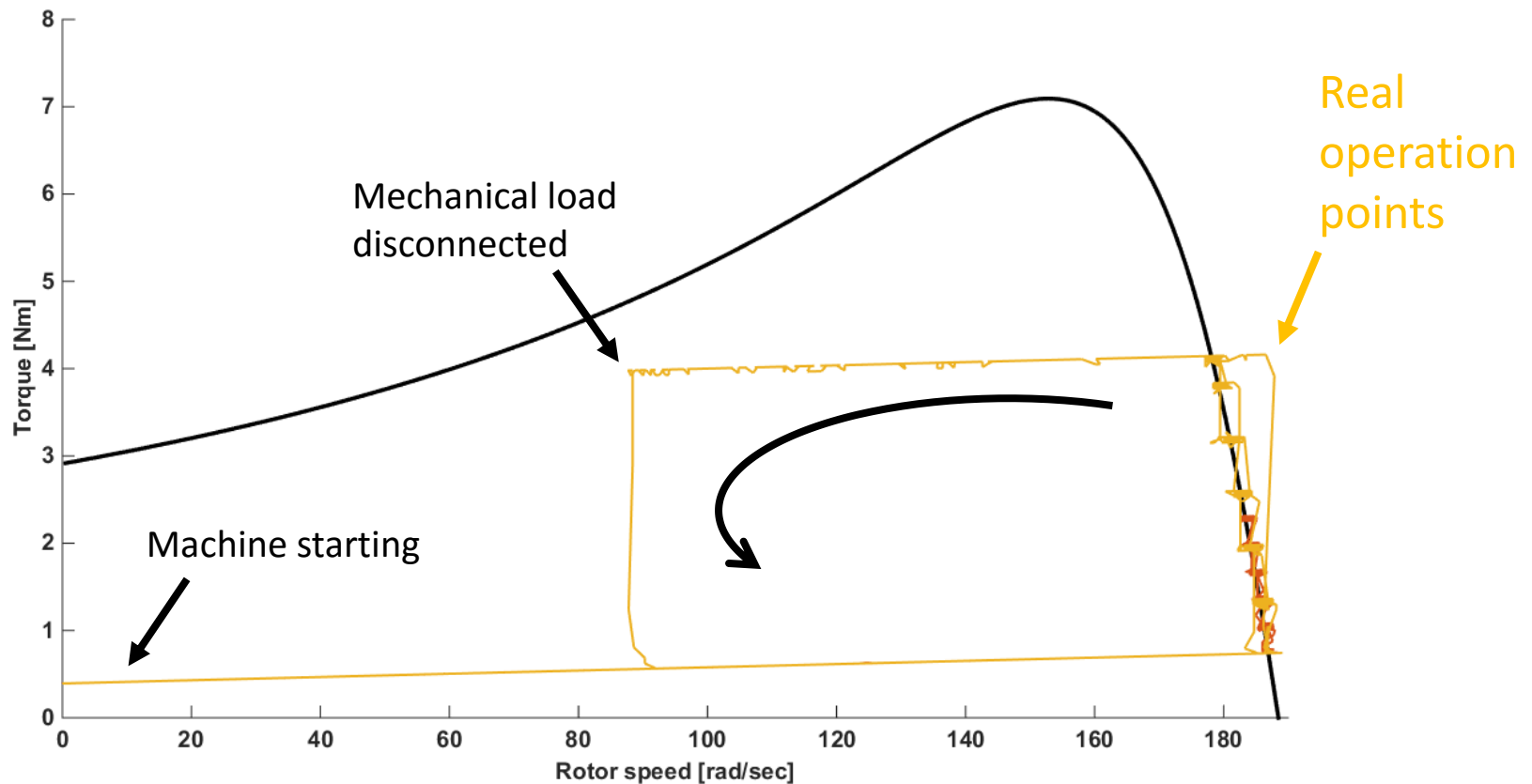






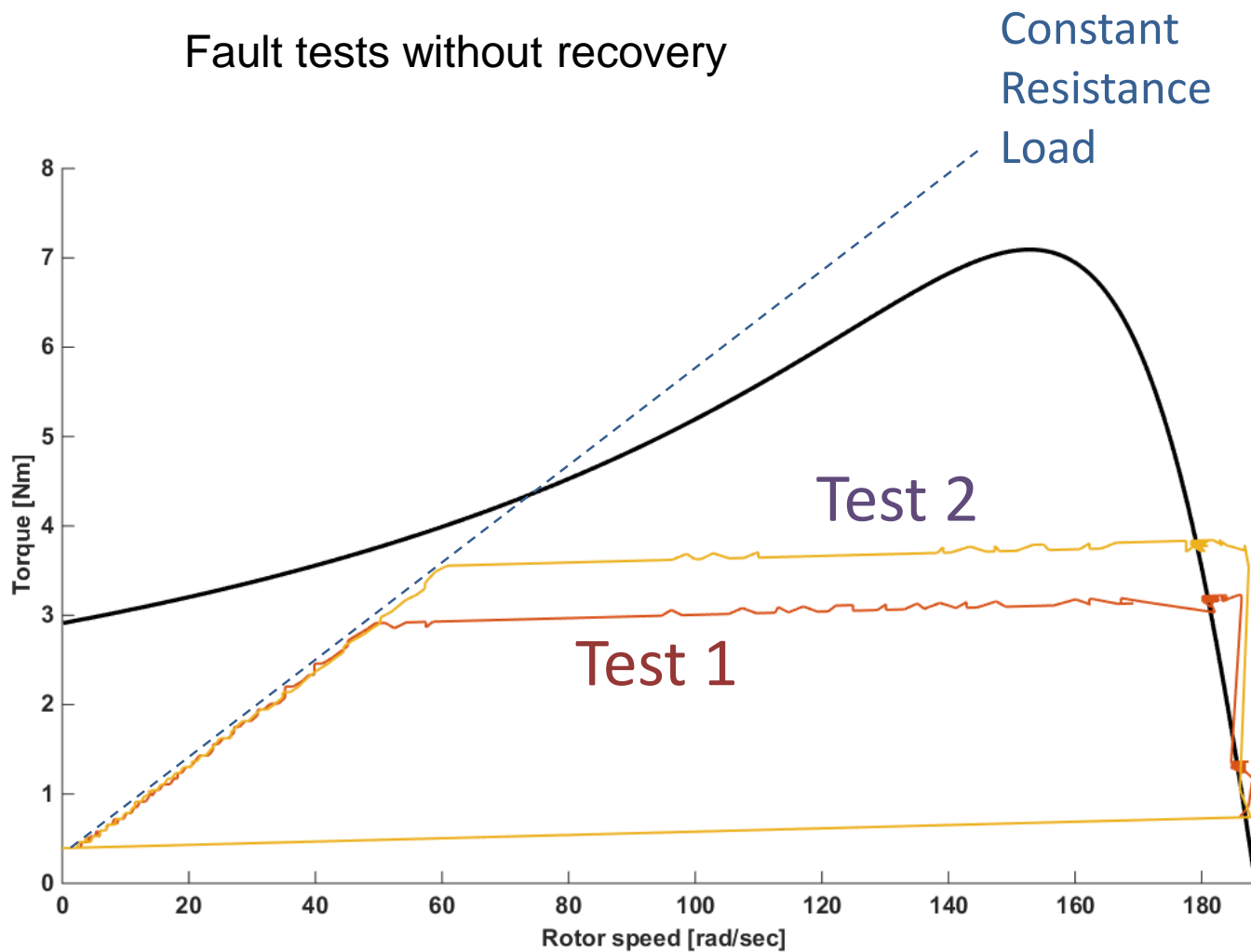
## Experimental Results

To validate the torque-speed curve, we did a load change experiment





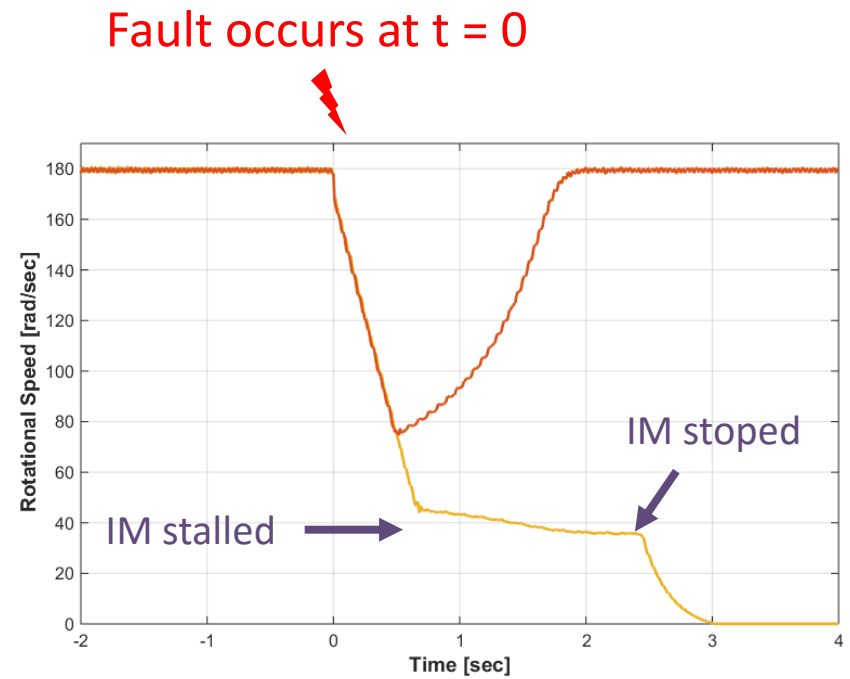
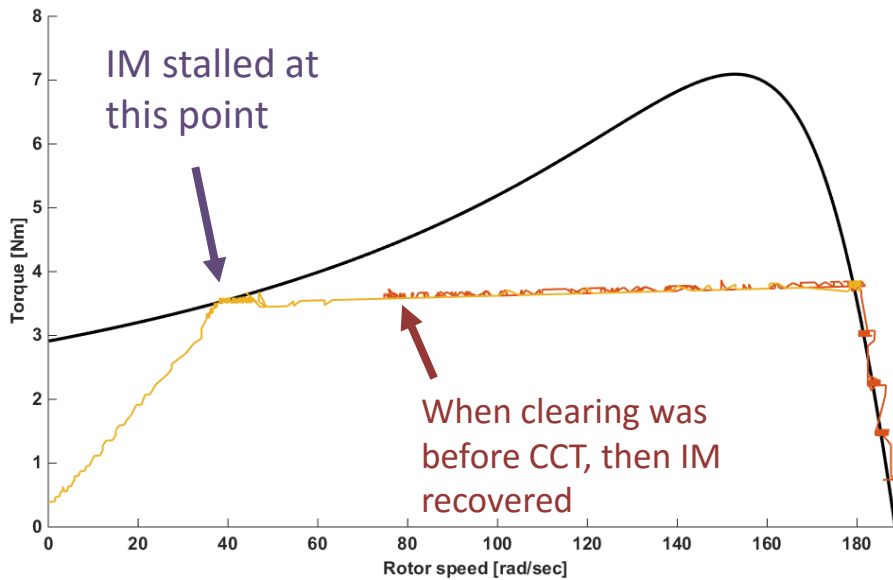
## Experimental Results





## Experimental Results

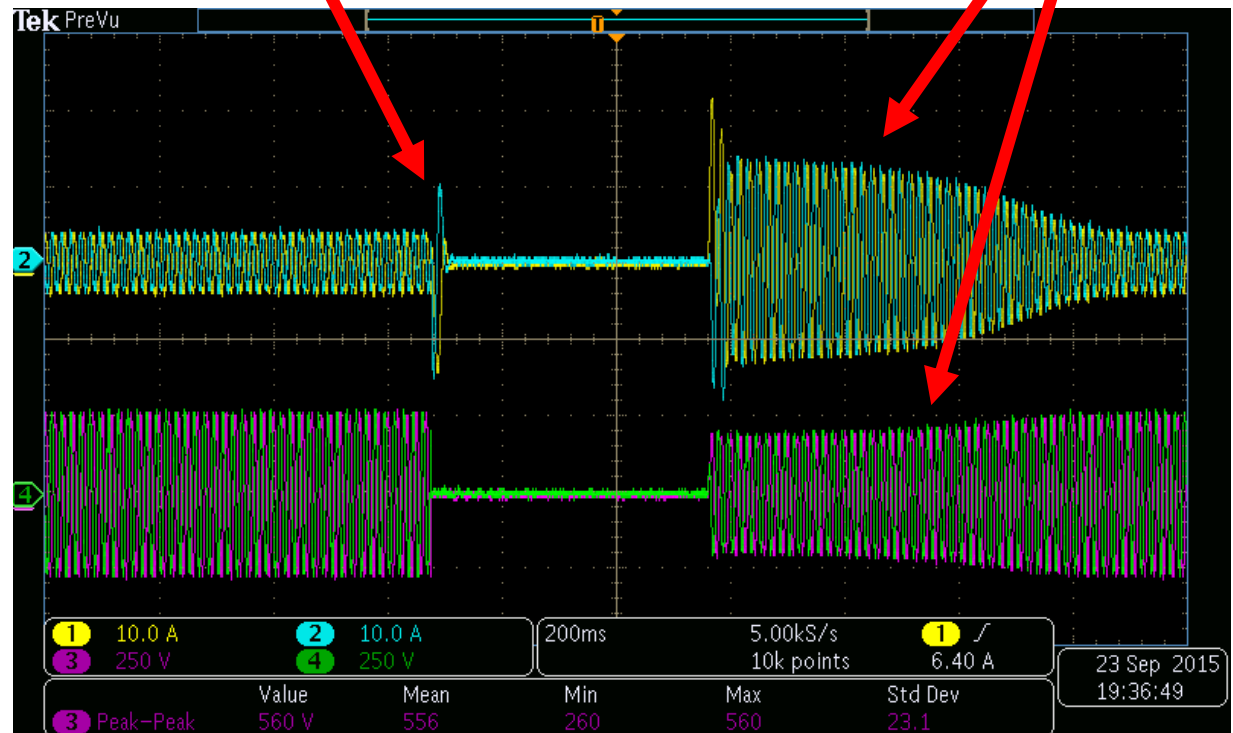
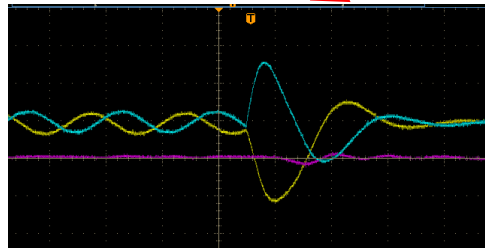
### Fault tests with recovery





## Experimental Results

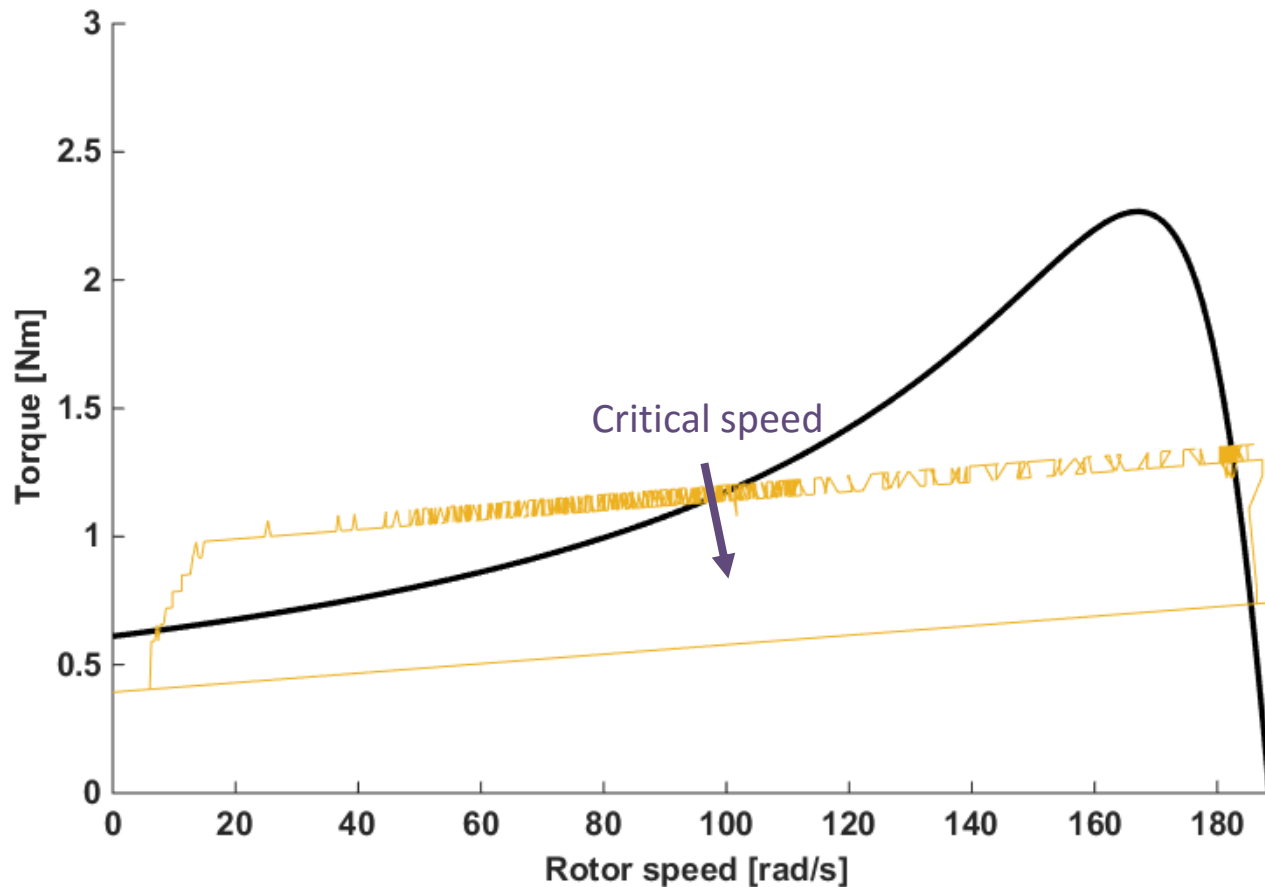
### Fault tests with recovery





## Experimental Results

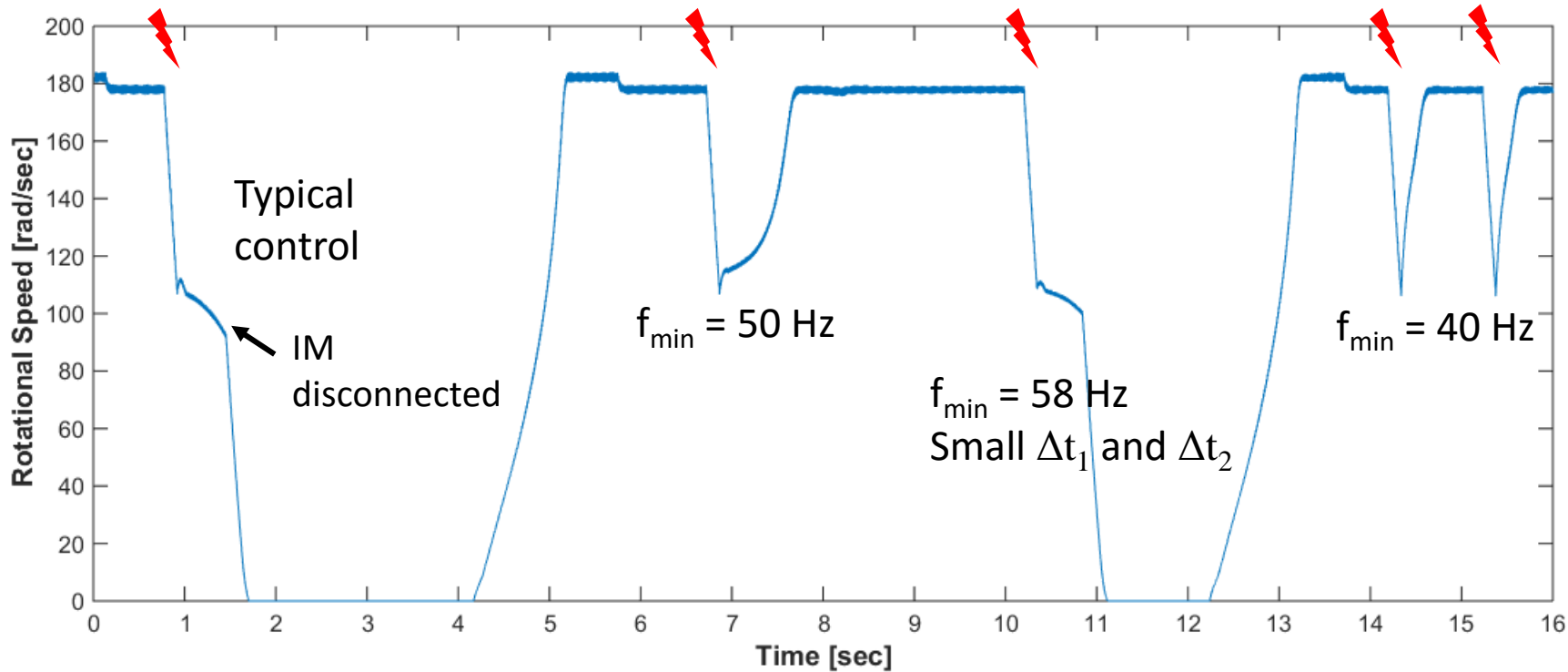
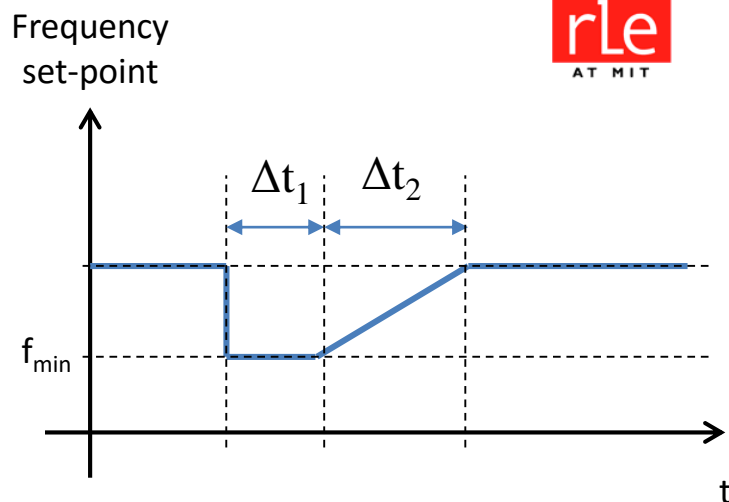
Inverter as source





## Experimental Results

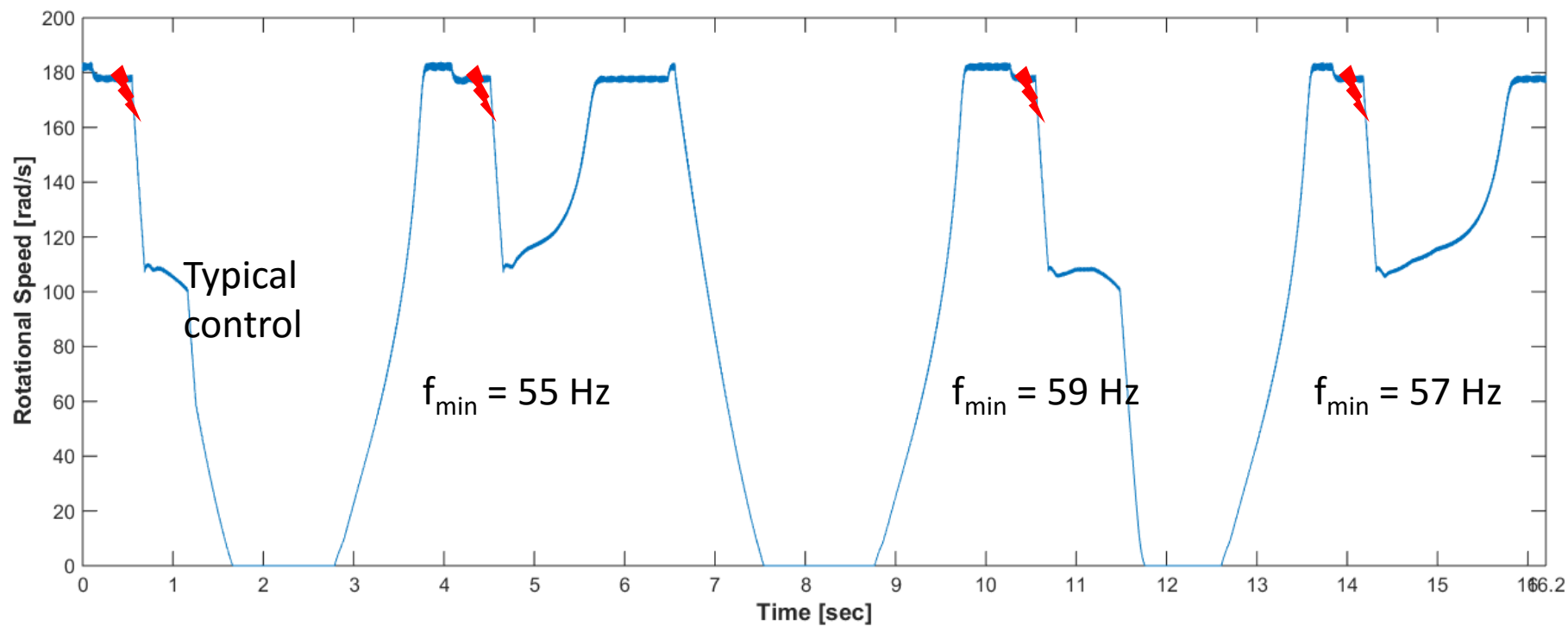
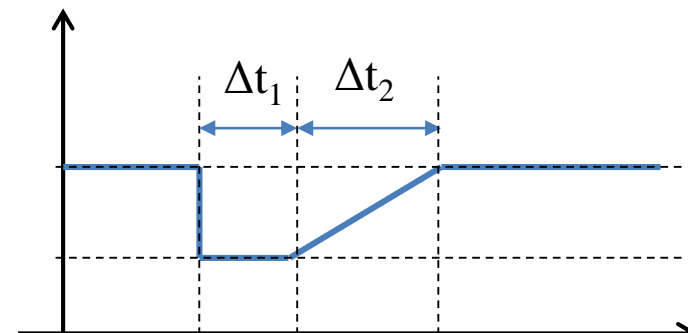
Inverter as source





## Experimental Results

Frequency  
set-point







## Conclusions

- Induction Motor (IM) are a significant fraction of loads in power systems and microgrids
- IM can stall leading to voltage collapse or load shedding
- Direct methods can be applied to calculate the CCT from machine parameters and initial conditions – *no need of time-domain simulations*
- A control strategy was proposed to increase the CCT and improve recovery
- Experimental results validate the above points